## 5. Exercise "Datenstrukturen und Effiziente Algorithmen", WS 18/19

Exercise 1: (5 Credits)
Construct for each $k \in\{0, \ldots, m-2\}$ a string of length $m$ such that its suffix tree has $k+m$ edges. Proof your result.

Exercise 2: (4.5+4.5+6=15 Credits)
Use the existence of a linear-time algorithm to construct a (compressed) suffix tree to show that the following problems can be solved in linear-time.
(a) Find all occurrences of pattern $P$ in a string $S$.
(b) Determine whether pattern $P$ occurs in all strings $S_{1}, \ldots, S_{\ell}$.
(c) Determine the longest substring of a string $S$ that occurs at least two times in $S$.

Exercise 3: (2.5+2.5=5 Credits)
Let $m$ be an arbitrary integer and $\mathcal{S}$ be the set of strings $S=s_{1} s_{2} \ldots s_{m}$ with $s_{i} \neq s_{m}=\$$, $1 \leq i<m$. Provide a string $S \in \mathcal{S}$ such that its implicit suffix
(a) has the fewest number
(b) has the largest number
of edges among all strings in $\mathcal{S}$. Proof your result.
HINT: Exercise 1

Exercise 4: (5 Credits)
Build the implicit suffixtree $\mathcal{T}$ of the string $S \$=$ TOCOTOC $\$$ using Ukkonens algorithm. Give for each phase $i+1$ and each extension $j$ where Rule 1 is not applied the respective "intermediate" trees.
Draw all suffix-links within your constructed $\mathcal{T}$.

