# 5. Exercise "Datenstrukturen und Effiziente Algorithmen", WS18/19

## **Exercise 1:** (5 Credits)

Construct for each  $k \in \{0, ..., m-2\}$  a string of length m such that its suffix tree has k + m edges. Proof your result.

### **Exercise 2:** (4.5+4.5+6=15 Credits)

Use the existence of a linear-time algorithm to construct a (compressed) suffix tree to show that the following problems can be solved in linear-time.

- (a) Find *all* occurrences of pattern P in a string S.
- (b) Determine whether pattern P occurs in all strings  $S_1, \ldots, S_\ell$ .
- (c) Determine the longest substring of a string S that occurs at least two times in S.

### **Exercise 3:** (2.5+2.5=5 Credits)

Let *m* be an arbitrary integer and S be the set of strings  $S = s_1 s_2 \dots s_m$  with  $s_i \neq s_m =$ \$,  $1 \leq i < m$ . Provide a string  $S \in S$  such that its implicit suffix

- (a) has the fewest number
- (b) has the largest number

of edges among all strings in S. Proof your result. HINT: Exercise 1

**Exercise 4:** (5 Credits)

Build the implicit suffixtree  $\mathcal{T}$  of the string S = TOCOTOC using Ukkonens algorithm. Give for each phase i + 1 and each extension j where Rule 1 is not applied the respective "intermediate" trees.

Draw all suffix-links within your constructed  $\mathcal{T}$ .

#### Deadline: Wednesday - November 21, 2018 - 12.15pm