Universität Greifswald Institute für Mathematik and Informatik Marc Hellmuth

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11. Übung "Bioinformatik", SS 16
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Aufgabe 1: (5 Credits)

Show that the two definitions for cographs are indeed equivalent:

**Def 1:** 

- $K_1$  is a cograph.
- The disjoint union of two cographs is a cograph.
- The complement of a cograph is a cograph.

## Def 2:

- $K_1$  is a cograph.
- The disjoint union of two cographs is a cograph.
- The join of two cographs is a cograph.

## **Aufgabe 2:** (5+5+5=15 Credits)

Let A, B, C, D be four different species from which we extracted some genetic material. In particular, we observed two independent gene families  $G^1$  and  $G^2$  consisting of the respective subsets  $G_X^1$  and  $G_X^2$  for each species  $X \in \{A, B, C, D\}$ .

Assume for the first family that  $G_A^1 = \{a_1, a_2\}, G_B^1 = \{b_1, b_2, b_3\}, G_C^1 = \{c_1\}, G_D^1 = \{d_1\},$ and the second family that  $G_A^2 = \{a'_1, a'_2\}, G_B^1 = \emptyset, G_C^1 = \{c'_1, c'_2\}, G_D^1 = \{d'_1, d'_2\}.$ 

Using multiple sequence alignments we obtained the following (symmetric) similarity scores for the genes in  $G^1$  and  $G^2$ :

$G^1$	$b_1$	$b_2$	$b_3$	$c_1$	$d_1$		$G^2$	$c'_1$	$c'_2$	$d'_1$	$d'_2$
$a_1$	-1	-1	-2	-2	-3	-	$a'_1$	-2	-3	-4	-4
$a_2$	-2	-2	-1	-2	-3		$a'_2$	-3	-2	-4	-4
$b_1$				-2	-2		$c'_1$			-2	-2
$b_2$				-2	-2		$c'_2$			-2	-2
$b_3$				-2	-2						
$c_1$					-1						

For simplicity, no two genes from different gene families will be estimated as orthologs or paralogs. Moreover, no horizontal gene transfer occurred.

- (a) Based on the similarity scores determine the estimated orthology relation  $\widehat{\Theta}_1$  and  $\widehat{\Theta}_2$  (for both gene families  $G^1$  and  $G^2$  independently) and show that  $\widehat{\Theta}_i$  (i = 1, 2) is a "valid" orthology relation.
- (b) Determine the event-labeled gene tree for each gene family.
- (c) Determine a possible species tree where the two gene trees evolved along and explain your result.

## Deadline: Monday - July 11th, 2016 - 2pm