

## 4. ÜBUNG "BIOINFORMATIK", SS 16

**Aufgabe 1:** (20 Credits)

Let  $X, Y, Z$  and  $Z'$  be distinct strings s.t. the set  $\{X, Y, Z, Z'\}$  is substring-free.  
Prove the following statement:

If  $\text{ov}(X, Y) \geq \max\{\text{ov}(X, Z), \text{ov}(Z', Y)\}$ , then  $\text{ov}(X, Y) + \text{ov}(Z', Z) \geq \text{ov}(X, Z) + \text{ov}(Z', Y)$ .

**Aufgabe 2: 10(+10)= (10 (20) Credits)**

Let  $S$  be a string that has periods of length  $p$  and  $q$  where  $q \leq p$  and  $|S| > p + q$ .

- (a) Show that  $S$  has a period of length  $p - q$ .
- (b) Show that  $S$  has a period of length  $\gcd(p, q)$ .

*Hint: Euclidean Algorithm*

Exercise (2b) is optional and you can get 10 bonus-credits.

**Deadline: Monday - May 2, 2016 - 2pm**