## 9. Exercise "Bioinformatics", SS 17

## Aufgabe 1: (3+2+5=10 Credits)

Given ordered forests  $F_1$ ,  $F_2$  and  $F_3$ . Let  $M_1$  be an ordered edit map from  $F_1$  to  $F_2$  and  $M_2$  be an ordered edit map from  $F_2$  to  $F_3$ . Prove:

- (a)  $M_1 \circ M_2$  is an ordered edit map from from  $F_1$  to  $F_3$
- (b)  $\gamma(M_1 \circ M_2) \leq \gamma(M_1) + \gamma(M_2)$

Let  $v_i$  be the root of the right-most tree in  $F_i$ , i = 1, 2. Prove:

(c) If  $v_1$  and  $v_2$  have both "partners" w.r.t. to an optimal map  $M_1$ , i.e.,  $(v_1, h), (k, v_2) \in M_1$ , then  $k = v_1, h = v_2$  and hence,  $(v_1, v_2) \in M_1$ .

## Aufgabe 2: (2+8=10 Credits)Given the secondary structures $S_1 = (\ldots)(\ldots)$ and $S_2 = ((\ldots))(\ldots)$

- (a) Give the tree representation  $T_1$ , resp.,  $T_2$  of  $S_1$ , resp.,  $S_2$  together with preordered labeled vertices.
- (b) Determine the tree edit distance of these trees (use the edit costs for RNA-trees as given in the lecture). Give the determined optimal ordered edit map and the respective sequence of edit operations that transform  $T_1$  into  $T_2$ .

Deadline: Tuesday - June 13, 2017